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# Oxide clusters as source of the third oxygen atom for the formation of carbonates in alkaline earth dehydrated zeolites

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## 1. Introduction

# The origin of the chemisorbed forms of  $CO<sub>2</sub>$  is a key question for modeling its possible chemical mechanisms of activation. In the case of zeolite frameworks, there is, to our best knowledge, still no clear answer about a microscopic model of  $CO<sub>2</sub>$  chemisorption for all classes of cation-exchanged zeolite form, involving transition metal, alkaline, and alkaline earth zeolites (AEZ). The  $CO<sub>2</sub>$ chemisorbed moiety can correspond to various carbonate species from a negligibly weak coordinated to the strongly coordinated toward one or more zeolite framework atoms. For simplicity, below in the article, we will use the term "carbonate" for all  $CO<sub>3</sub>$  moieties independently of their coordination number. Even if numerous assignments of IR spectroscopic data have already been published for those materials [\[1–6\],](#page-9-0) a final explanation about the carbonate formation remains indeed ambiguous.

# **ABSTRACT**

In our paper, we show that carbonates can be formed with almost no energetic barrier from  $CO<sub>2</sub>$  and metal-oxide binuclear MO<sub>X</sub>M species (M = Mg, Ca, Sr, Ba, with  $X = 1-4$ , depending on the cation) in alkaline earth zeolites, mordenite (MOR) and phillipsite (PHI), on the basis of quantum mechanical density functional theory (DFT) calculations at both isolated cluster and 3D periodic levels. The participation of MO<sub>x</sub>M species (X = 1 and 3) explains the source of the third O atom in CO<sub>3</sub> species in dehydrated zeolites, on the basis of a good agreement between the calculated and experimental positions of the asymmetric and symmetric  $CO<sub>3</sub>$  vibration bands, of the ratio of their intensities, and of the weak dependence versus the cation and framework type. The reaction of formation of dimethylcarbonate from  $CaCO<sub>3</sub>Ca$  in the 8-membered (8R) ring of MOR and methanol has also been considered, suggesting the carbonate activity as the source of  $CO<sub>2</sub>$  at elevated temperatures.

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Early studies  $[1,2]$  mentioned differences between  $CO<sub>2</sub>$  adsorbed in the Mg form and in the other AEZ. However, this difference was later denied by the work of Jacobs et al. [\[3\]](#page-9-0) who registered similar IR bands of carbonates, in particular, in CaX zeolite. The influence of the cation type was shown in Ref. [\[4\]](#page-9-0) regarding rather moderate variations of the most intense IR band positions. Additionally, weak or at least non-clear dependences of the zeolite framework type (the MgETS-10 zeolite) for similar strong bands manifested at 1620 and 1380  $cm^{-1}$  were noticed in Ref. [\[6\]](#page-9-0). A strong doublet at 1665 and 1325  $cm^{-1}$ , conserved in the spectra up to 500 $\degree$ C, was assigned to carbonate species similar to the one over an MgO surface [\[7\]](#page-9-0), while a less stable doublet at  $1620/1370$  cm<sup>-1</sup> disappears when the temperature rises above 200 $\degree$ C over MgO. Starting from the assignment available in Ref. [\[8\]](#page-9-0), the higher and lower frequencies of the  $CO<sub>3</sub>$  group were attributed to symmetric and asymmetric carbonate vibrations, respectively [\[3,4\]](#page-9-0). A ratio of the higher/lower band intensities was published in Ref. [\[4\]](#page-9-0). Going forward, we should note that our assignment of the symmetric and asymmetric carbonate vibrations for the lower and higher branches is inverted versus the conventional interpretation [\[3,4\]](#page-9-0).

An important chemical problem behind our assignment proposed here just above is the origin of the third O atom in the  $CO<sub>3</sub>$ species. In hydrated forms, it is obvious that the water oxygen can be involved in the  $CO<sub>3</sub>$  formation. For dehydrated zeolites,



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<span id="page-1-0"></span>two possibilities were discussed in the literature [\[3,6\].](#page-9-0) Either the framework O atoms or the oxo-species can be the source of the third O for the carbonates. On the one hand, the similarity between the various O types denied the suggestion about the participation of the framework oxygens in the carbonate structure [\[6\]](#page-9-0). On the other hand, some of us recently considered CO oxidation on binuclear MO<sub>X</sub>M clusters ( $X = 2-3$ ) in AEZ at both the isolated cluster [\[9,10\]](#page-9-0) and periodic [\[11\]](#page-9-0) calculation levels. It was shown that the products of CO oxidation transform via a barrierless reaction profile to carbonates. The present work actually adds evidence for the hypothesis about the oxo-species as the source of O for carbonates. Till now, to our knowledge, no theoretical study proposed a clear explanation of the experimental data obtained so far. The assignment of the carbonate frequencies could thus help to understand the carbonate formation mechanism. The comparison of the IR bands is therefore the main goal of this paper. More precisely, we optimized the structure of the products of the interaction between the MO<sub>x</sub>M species (M = Mg, Ca, Sr, Ba, with  $X = 1-4$ ) and  $CO<sub>2</sub>$  and calculated the respective frequencies at both the isolated cluster and periodic DFT levels.

### 2. Computational details

First, we applied the isolated cluster approach, considering Gaussian 03 [\[12\],](#page-9-0) to check the possibility of carbonate formation over an isolated cation or cluster, as well as to further calculate the frequencies and intensities of the carbonate species in an 8 membered ring (8R) as found in mordenite (MOR) and in a fragment that includes two 6R and 4R windows  $(6R + 4R)$  with one common Si–O–Si moiety for zeolite Y. Initial chemical compositions of the cluster models (without carbonate species) are MAl2-  $Si<sub>6</sub>O<sub>8</sub>H<sub>16</sub>$  and  $MAI<sub>2</sub>Si<sub>6</sub>O<sub>9</sub>H<sub>14</sub>$  for 8R and 6R + 4R, respectively, where M is the AE cation. Two Al atoms are present in both 8R and  $6R + 4R$  models as in our previous work  $[9-11]$ . Most of the results were obtained at the B3LYP/6-31G\* level, while a higher MP2/ 6-31G\* level was applied in some cases. To determine the reaction coordinate for  $CO<sub>2</sub>$  or carbonate reaction with methanol (see Section [4](#page-8-0)), we applied the QST3 algorithm as supplied with Gaussian 03 considering the optimized geometries of both the reagents and products.

Second, for the periodic approach, we optimized the cell parameters and the geometries of the  $MO_XM(MOR)$  and  $MO_XM(PHI)$  moieties (M = Mg, Ca, with  $X = 1-4$ ) using VASP [\[13\].](#page-9-0) The projector augmented wave (PAW) method [\[14\]](#page-9-0) was used to describe the electron–ion interactions, and a plane-wave basis set was employed for the valence electrons. The plane-wave cutoff was set to 500 eV. Results were obtained with the PBE and PW91 generalized gradient approximation (GGA) functionals [\[15\].](#page-9-0) The Brillouin zone sampling was restricted to the  $\Gamma$ -point. The chemical composition of the unit cell is  $MAl_2Si_{46}O_{96}$  for MMOR and  $M_2Al_4Si_{12}O_{32}$ for MPHI. The compositions including the  $MO_XM$  moieties correspond to  $(MO_XM)Al_2Si_{46}O_{96}$  and  $(MO_XM)_2Al_4Si_{12}O_{32}$ , respectively. The optimized cell parameters are given in Table 1. After optimization of the  $MO_XM(MOR)$  moiety, we added  $CO_2$  and performed the optimization of the entire systems. Vibrational frequencies were calculated using the finite difference method as implemented in VASP. Small displacements (0.015 Å) of the atoms from the  $MCO<sub>3</sub>M(MOR)$  species were used to estimate the numerical Hessian matrix. The rest of the zeolite atoms were kept fixed at their equilibrium positions. As any theoretical approach results in frequency values shifted relative to the experimental data, we scaled all frequencies by fitting one band position  $v_{cal}$  to the experimental  $v_{\rm exp}$  value and then recalculated the positions of the other bands multiplying them by ( $v_{exp}/v_{cal}$ ). Regarding that the frequencies obtained with B3LYP are pretty similar to the experimental ones, we

#### Table 1

Unit cell parameters (a, b, c, in Å,  $\alpha$ ,  $\beta$ ,  $\gamma$ , in degrees) and cell volumes (in  $\AA^3$ ) of MOR and PHI type zeolites as optimized at (PW91) level.



rescaled only the frequencies calculated at the periodic level with PW91. In order to check the accuracy of the projected densities of states (PDOS) of the CaO<sub>3</sub>Ca and CaOCa +  $O_2$  complexes in MOR, we considered different (2, 2, 2) and (3, 3, 3) sets of shrinking factors. The s-, p-, and d-orbitals for selected Ca, Al, and O atoms were projected in both the singlet and triplet states that possess similar (CaO<sub>3</sub>Ca) or essentially different (CaOCa + O<sub>2</sub>) relative stability. Visualization at both cluster and periodic theoretical levels was realized with the MOLDRAW code [\[16\].](#page-9-0)

#### 3. Results

# 3.1. Consideration of the framework oxygen for the carbonate formation

To test the possibility of carbonate formation involving a framework oxygen of the zeolite cationic form without any  $MO_XM$  species, a series of optimization was performed considering one M cation with both 8R and  $(6R + 4R)$  cluster models for all M = Mg, Ca, Sr, and Ba. More precisely, we looked for a geometry in which the carbonate is formed with a third O atom of the framework owing to a partial weakening of its binding to the neighbor T atoms. No carbonate structure could be obtained. Only a linear  $CO<sub>2</sub>$  geometry with a maximal distortion of  $169.8^\circ$  was observed for the Mg(8R) cluster in MOR (Fig. 1). The weakness of  $CO<sub>2</sub>$  interaction with the framework oxygen in alkali form zeolites was already discussed [\[17\]](#page-9-0). The authors concluded as well that carbonate formation should not be observed in regards of the weak interaction between  $CO<sub>2</sub>$  and the framework oxygen in this type of zeolites.

## 3.2. Consideration of the oxygen of metal oxide species for the carbonate formation

#### 3.2.1. Isolated cluster approach

We next studied the reactions between  $CO<sub>2</sub>$  and the  $MO<sub>X</sub>M$  species. The Ca cluster geometries were already described in details



Fig. 1. Optimized structure of the product of  $CO<sub>2</sub>$  interaction with the Mg(8R) moiety in MOR, as calculated at the B3LYP/6-31G\* level. The color code is O in red, Si in yellow, Al in violet, Ca in blue, C in brown, and H in gray. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

<span id="page-2-0"></span>[\[9,10\].](#page-9-0) The product of the interactions between  $CO<sub>2</sub>$  and CaOCa(8R) or BaOBa(8R) as obtained at the B3LYP/6-31G\* level is shown in Figs. 2a and b. The positions of the Mg cations and geometries of the  $MO_XM$  species were calculated at the cluster and periodic levels, including the carbonate species [\[11\]](#page-9-0). We modeled the tetradentate carbonate type with three O atoms coordinated toward two M atoms of the MOM cluster. One O is bi-coordinated toward two M atoms, and two others are mono-coordinated toward one M atom (Fig. 2a). Earlier interpretations suggested that mono- and bidentate  $CO<sub>3</sub>$  groups coordinated to only one cation by either one or two O atoms are presented in zeolites [\[1–7\]](#page-9-0). Higher coordination numbers were suggested in alkali zeolites with a higher quantity of monovalent (Na) cations per cell as compared to AEZ, without, however, a respective analysis of the IR spectra [\[6\].](#page-9-0)

The vibrational frequencies of the carbonate anion were calculated for the isolated  $MgCO<sub>3</sub>Mg(6R + 4R)$  cluster as 1329.5/ 1645.8 cm<sup>-1</sup> for the symmetric/asymmetric vibrations (Table  $2<sup>4</sup>$ ), respectively, in qualitative agreement with the experimental values, 1734, 1700, 1625, 1382, and 1363  $cm^{-1}$ , assigned to carbonate in MgX [\[2\]](#page-9-0) as well as with 1620 and 1380  $\rm cm^{-1}$  in MgETS-10 [\[6\]](#page-9-0). Similar asymmetric/symmetric doublets were obtained considering other cations [\(Table 2\)](#page-3-0), thereby confirming a weak dependence of the band positions versus the cation type. For the obtained tetra-dentate carbonate structure (Fig. 2a and b), its symmetric vibration is more strongly suppressed and red shifted versus the asymmetric one as mentioned over alumina [\[18\].](#page-9-0) The tetra-dentate structure allows to find the explanation for the ratio between the intensities of the symmetric and asymmetric vibrations versus the usually inverted ones for the respective carbonate vibrations in the gas state.

A tri-dentate structure has been obtained for the products of  $CO<sub>2</sub>$  interaction with the CaO<sub>2</sub>Ca(8R) (Fig. 2c) and CaO<sub>2</sub>Ca(6R + 4R) (Fig. 2d) complexes at the B3LYP/6-31G\* level  $(X = 2$  in [Table 2\)](#page-3-0). The two asymmetric and symmetric vibration bands for the tridentate carbonate are shifted to higher, 1869–1960 cm $^{-1}$ , and lower, 1260–1304 cm $^{-1}$ , frequencies *versus* those of the tetra-dentate ones, respectively. Experimentally, it is difficult to register the low-frequency branch of the doublet near 1200 cm $^{-1}$  owing to the intensive framework Si–O–Si vibrations [\[19\]](#page-9-0). The high-frequency branch is outside the conventional range from 1800 to 1200  $\text{cm}^{-1}$  for carbonates [\[1–7\]](#page-9-0). It seems that tri-dentate forms do not appear in most zeolites owing to their lower stability as compared to the tetra-dentate ones obtained with the CaOCa and CaO<sub>3</sub>Ca moieties for both  $(6R + 4R)$  and 8R type rings. The heats of carbonate formation were calculated, for example, for the  $CaO<sub>X</sub>$ -Ca(8R) cluster as  $-72.3$  (X = 1) and  $-20.4$  (X = 2) kcal/mol at the B3LYP level, and as  $-77.1$   $(X=1)$  and  $-19.9$   $(X=2)$  kcal/mol at the MP2 level. The two bands positioned at 1850/1180  $\rm cm^{-1}$  and assigned to the asymmetric/symmetric modes of carbonate, respectively, suggest the presence of a tri-dentate carbonate over an alumina surface [\[18\]](#page-9-0).

As our computations led to the triplet state as the most stable for the  $MgO_3Mg(6R + 4R)$  cluster, the latter was not considered in this study. We considered  $CO<sub>2</sub>$  addition to  $CaO<sub>3</sub>Ca(6R + 4R)$  only. We observed the formation of the tetra-dentate  $CaCO<sub>3</sub>Ca(6R + 4R)$ carbonate, *i.e.*, the product of  $CO<sub>2</sub>$  addition to  $CaOCa(6R + 4R)$ , and simultaneously the formation of an  $O<sub>2</sub>$  fragment coordinated to the upper Ca cation.

The stability of metal-oxide binuclear  $MO_XM$  species was confirmed experimentally for  $M = Ga$  [\[20\],](#page-9-0) while it was considered as doubtful for ZnOZn on the basis of computational results [\[21\].](#page-9-0) Not knowing any discussion regarding the AEZ  $MO_XM$  species, we have recently evaluated the reactions of their formation at



Fig. 2. Optimized structures of the products of  $CO<sub>2</sub>$  interaction with the CaO<sub>X</sub>Ca(8R) (a:  $X = 1$  and c:  $X = 2$ ) moieties in MOR, (b) BaOBa(8R) moieties in MOR, and (d)  $CaO<sub>2</sub>Ca(6R + 4R)$  moieties in FAU, as calculated at the B3LYP/6-31G\* level. The color code is the same as in [Fig. 1,](#page-1-0) Ba in light blue. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

 $4$  For shortness in [Table 2,](#page-3-0) we compare the experimental data for CaX from Ref. [\[4\]](#page-9-0) keeping in mind the similarity between the X and ETS-10 zeolite framework types and the cationic forms.

#### <span id="page-3-0"></span>Table 2

Band positions (cm<sup>-1</sup>) of the asymmetric ( $v_{\rm asym}$ ) and symmetric ( $v_{\rm sym}$ ) vibrations as well as the intensity ratios ( $I_{\text{asym}}/I_{\text{sym}}$ ) for the carbonate species in the MO<sub>X</sub>M(6R+4R) cluster ( $M = Mg$ , Ca, Sr, Ba) calculated at the B3LYP/6-31G\* level compared to the experimental data for  $X = 1$  [\[4\]](#page-9-0) and  $X = 2$  [\[18\].](#page-9-0)

	Mg	Ca	Sr	Ba	Experiment
$X = 1$					
$v_{\text{asym}}$	1645.8	1664.0	1663.0	1651.0	1700, 1665, 1625 <sup>a</sup>
$v_{sym}$	1329.5	1333.7	1335.9	1342.6	1365, 1390, 1440 <sup>a</sup>
$I_{\rm asym}/I_{\rm sym}$	1.24	1.62	1.37	1.37	$1.45 - 1.55^a$
$X = 2$					
$v_{\text{asym}}$	1912.0	1959.7	1874.7	1868.7	1850 <sup>b</sup>
$v_{sym}$	1260.0	1267.7	1279.3	1303.5	1180 <sup>b</sup>
$I_{\text{asym}}/I_{\text{sym}}$	1.16	1.31	1.47	2.50	

Upper  $v_{\text{asym}}$  and lower  $v_{\text{sym}}$  values correspond to the three doublets in CaX zeolite [\[4\]](#page-9-0).

**b** For alumina [\[18\].](#page-9-0)



**Fig. 3.** Electron densities ( $e \times \text{\AA}^{-3}$ ) at the critical points between the Na (triangles down) or Ca (triangles up) cations and the zeolite framework (open symbols) or carbonate (closed symbols) oxygens versus the M $\cdots$ O distance (Å) calculated in the neutral (Na $\cdot\cdot$  O(0)) or charged (Na $\cdot\cdot$  O(-2)) 6R + 4R and 8R clusters, respectively, at the MP2/6-31G\* level.

the cluster [\[9,10\]](#page-9-0) and periodic [\[11\]](#page-9-0) levels as exothermic. The formation of the carbonates can serve as a confirmation of the presence of metal-oxide binuclear  $MO_XM$  species in the AEZ forms. Such explanation can be confirmed via the comparison of the electron densities (ED) at the bond critical points (CPs) between the cations and the framework  $O_{\text{zeo}}$  or carbonate  $O_{\text{carb}}$  oxygens. The ED difference illustrates the relative strength of the bonds. Would the bond  $M-O<sub>carb</sub>$  be stronger than the  $M-O<sub>zero</sub>$  one, then we could admit that carbonate is not anchored to the framework and hence could move together with one or two cations. In such a way, carbonate could gradually trap the first cation and then, after a drift, trap the second one. To elucidate this possibility, we calculated the CPs and ED values using Bader AIM theory [\[22\]](#page-9-0) as supplied with the Gaussian code.<sup>5</sup> The ED difference at the M-O<sub>carb</sub> (Fig. 3, closed triangles) and  $M-O<sub>zen</sub>$  (Fig. 3, open triangles) bonds is rather small to justify such model. Hence, we cannot approve the mobility of the carbonate species in the AEZ lattice. For comparison, this last conclusion does not suit for carbonates with alkali cations. The difference between the EDs of the Na– $O_{\text{carb}}$  and Na– $O_{\text{zero}}$  bonds is also

emphasized (Fig. 3, open and closed circles), similarly for lower ED values relative to the ones that obtained for the AEZ carbonates. The lower potassium bonding with the framework results in a higher cation mobility together with the carbonates, as found experimentally [\[24–26\]](#page-9-0) and interpreted for the mixed NaKA zeolite [\[23\]](#page-9-0). It also signifies that the AEZ carbonate formation can happen at two AEZ cations that are closely located as parts of the binuclear  $MO_XM$  species. That is why we consider the AEZ carbonate formation as the indirect confirmation of the  $MO_XM$  presence in AEZ. Mixed earth alkaline (M)–alkali (M') carbonates (MCO<sub>3</sub>M') are also immobile in the zeolites. Such species appear, for example, in the course of partial sodium exchange and present similar vibrational spectra [\[27\]](#page-9-0).

#### 3.2.2. Periodic approach

# 3.2.2.1. Heat of formation and favored multiplicity of the  $MO_xM$ species at the periodic computational level.

3.2.2.1.1. CaO<sub>x</sub>Ca species in mordenite (MOR). In order to model the carbonate formation, we needed to determine the ground state of each of the considered systems. Structural and energetic aspects at the isolated cluster computational level have already been pre-sented [\[9–11\].](#page-9-0) The favored multiplicity of each  $CaO<sub>x</sub>Ca$  species was determined by the sign of the  $\Delta U_{ST}$  difference between the total energies of the singlet and triplet states ( $\Delta U_{ST}$  =  $U_S - U_T$ ), a positive value corresponding to a favored triplet state ([Table 3\)](#page-4-0). The signs of the  $\Delta U_{ST}$  values vary with X. We remind that at the cluster level,  $\Delta U_{\rm ST}$  was negative for Ca for any X = 1–4 values,  $^6$  while  $\Delta U_{\rm ST}$  was negative for Mg for  $X = 1-2$  only. For Sr and Ba, an intermediate situation was observed, i.e.,  $\Delta U_{ST}$  < 0 for X = 1–3. Herein, we additionally discuss for the first time the favored multiplicity of the  $CaO<sub>x</sub>Ca$  species in zeolites at the periodic computational level.

One of the sharp differences between the cluster and periodic models resides in the respective  $\Delta U_{ST}$  values ([Table 3](#page-4-0)). A non-correct estimation is obtained at the cluster level for the triplet CaOCa(8R) moiety only. The exaggerated  $\Delta U_{ST}^{\rm CL}$  difference between the singlet and triplet energies at the cluster level  $(-118.0 \text{ kcal/mol})$ with MP2) relative to the periodic values  $(-0.39$  and  $-0.30$  kcal/ mol with PW91 and PBE, respectively) is the result of a strong distortion of the triplet CaOCa(8R) moiety and of the localization of the spin density at the capping H atom. The maximal spin density is concentrated at the capping H atom  $(0.916 e)$  closest to the Ca cation (0.916  $e$ ) that is detached from the O atoms of the 8R ring ([Fig. 4a](#page-5-0)). Only a minor spin density  $(0.105 e)$  is concentrated at the second Ca cation of the Ca–O–Ca bridge. It is a rare case when the computations of the electron correlation at the MP2 level result in a worse  $\Delta U_{\textrm{ST}}^{\sf CL}$  as compared to DFT. For comparison, calculations with B3LYP do not shift the spin density to the capping H atom and give  $\Delta U_{\text{ST}}^{\text{CL}}$  =  $-55.8$  kcal/mol. We did not include the triplet CaOCa(6R + 4R) cluster case in [Table 3,](#page-4-0) but MP2 also resulted in an exaggerated  $\Delta U_{\rm ST}^{\rm CL}$  difference of  $-134.4$  kcal/mol. In this last case, the bond of the capping H atom near Al is strongly elongated (isolated H atom in the lower left corner of [Fig. 4d](#page-5-0)) so that Al becomes tricoordinated. And again, the triplet CaOCa(6R + 4R) cluster presents normal lengths of all T–H bonds (T = Al, Si), when optimized using B3LYP [\(Fig. 4d](#page-5-0)). The problem of the triplet  $MO_XM$  distorted geometry obtained at the MP2 level, however, disappears with higher X values. For the triplet  $CaO<sub>2</sub>Ca(8R)$  already, the spin density is only concentrated on the oxygen atoms (1.032 e) that do not form an O– O bond, whereas minor density values correspond to the Ca cations (both  $-0.040$  e). The difference between the singlet and triplet geometries of  $CaO<sub>2</sub>Ca(8R)$  resembles to the geometries of the  $CuO<sub>2</sub>$ Cu models [\[6,7\]](#page-9-0) with one O–O bond present in one of them,  $(\mu \eta^2$ : $\eta^2$ -peroxo)dicopper, only.

<sup>&</sup>lt;sup>5</sup> The ED values in Fig. 3 are given for charged  $NaCO<sub>3</sub>Na(6R + 4R)<sup>2–</sup>$  cluster but similar ED differences remain if one uses neutral and all-siliceous 6R + 4R clusters. For the neutral case (with two H atoms in the 6R + 4R cluster), the higher mobility of the sodium carbonate results in its displacement towards one O atom of the carbonate coordinated to one of the protons in the 6R. The ED comparison is therefore not straightforward. More details about the Na clusters are given in Ref. [\[23\]](#page-9-0).

<sup>&</sup>lt;sup>6</sup> For  $X = 4$ , no  $\Delta U_{ST}$  was calculated but the singlet state is stable as compared to the triplet one for which no convergence was achieved.

#### <span id="page-4-0"></span>Table 3

Relative and absolute energies (eV) of the singlet (U<sub>S</sub>) and triplet (U<sub>T</sub>) states of the O<sub>2</sub> molecule as well as of the MOR and PHI unit cells including the CaO<sub>X</sub>Ca and MgO<sub>X</sub>Mg species, singlet–triplet energy differences ( $\Delta U_{\rm ST}$  =  $U_{\rm S}$  –  $U_{\rm T}$ , kcal/mol),  $\Delta U_{\rm ST}^{\rm GL}$  (kcal/mol) at the B3LYP and PW91 levels of the isolated 8R cluster [\[9–11\]](#page-9-0), and heats  $\Delta U$  of the reaction (1)and (kcal/mol) between singlet states using VASP (PW91).

Species	$U_s$ PW91	$U_T$ PW91	$\Delta U_{ST}$ PW91	$\Delta U_{ST}$ PBE	$\Delta U_{\text{CT}}^{\text{CL}}$ PW91	$\Delta U_{\text{ST}}^{\text{CL}}$ B3LYP	$\Delta U$
0 <sub>2</sub>	$-8.750$	$-9.766$	23.65	25.14	41.37	33.12	
<b>MOR</b>							
CaOCa	$-1160.064$	$-1160.047$	$-0.39$	$-0.30$	$\mathbf{C}$	$-55.8, -118.0$	
CaO <sub>2</sub> Ca	$-1165.561$	$-1165.545$	$-0.37$	$-0.27$	$-26.2$	$-31.2, -41.9b$	$-14.04$
CaO <sub>3</sub> Ca	$-1170.389$	$-1170.409$	0.46	0.31	$-21.1$	$-14.2$	1.38
$CaOCa + O2$	$-1168.987$	$-1169.361$	8.62	10.00	$\overline{\phantom{0}}$	-	19.67
CaO <sub>4</sub> Ca	$-1175.721$	$-1175.722$	0.02	0.06	$-8.4$	$\mathbf{C}$	$-10.23$
PHI <sup>d</sup>							
MgOMg	$-403.543$	$-403.544$	0.01	0.00	-	$\mathbf{C}$	
MgO <sub>2</sub> Mg	$-413.710$	$-413.711$	0.01	0.01	-	$-$ <sup>c</sup> , $-$ 43.5 <sup>b</sup>	$-4.51$
MgO <sub>3</sub> Mg	$-422.571$	$-422.570$	$-0.01$	0.00	$\overline{\phantom{0}}$	9.9, $10.2b$	10.55
$MgOMg + O2$	$-422.734$	$-423.334$ <sup>e</sup>	6.92	8.24	$\overline{\phantom{0}}$	$\qquad \qquad -$	4.17
MgO <sub>4</sub> Mg	$-431.407$	$-431.410$	0.03	0.04	-	19.6	10.84
$MgO2Mg + O2$	$-432.491$	$-433.701^e$	13.95	14.67	-	$\qquad \qquad -$	8.89

<sup>a</sup> the steps for reaction (1) at  $X = 2-4$  for Ca are illustrated in [Fig. 6](#page-6-0).

 $b$  MP2/6-31G\* level.

 $c$  no SCF convergence while using B3LYP/6-31G\* for triplet states.

<sup>d</sup> the energy corresponds to two MgO<sub>X</sub>Mg species per PHI cell, so that the  $\Delta U_{ST}$  and  $\Delta U$  values are divided per two. <sup>e</sup> for non-symmetric cell (P1 group).

The energy difference between the singlet and triplet  $MO_XM$ states disappears while going from the cluster calculations to the periodic models using VASP for the MOR or PHI zeolites (Table 3). It can be confirmed by comparison between the projected densities of states (PDOS) of the singlet and of the triplet states of similar atoms in the different systems. For example in [Fig. 5](#page-5-0)a, we compare the PDOS of the sum of the up and down spin states at the O97 atom, the side atom in the  $CaO<sub>3</sub>Ca$  moiety, to the total PDOS value of the singlet  $CaO<sub>3</sub>Ca$  species for MOR (right lower corner in [Fig. 6\)](#page-6-0), for which the energies of the triplet and singlet  $CaO<sub>3</sub>Ca$  moieties are pretty close (0.46 kcal/mol at the periodic PW91 level, Table 3). The difference between the PDOS values is minor for all the Ca, O, and Al atoms.<sup>7</sup> On the opposite, a sharper difference is noted between the PDOS values on the O97 atom in the singlet and triplet states of the Ca–O97–Ca +  $O_2$  system ([Fig. 5b](#page-5-0)) which is more stable in the triplet state by 8.62 kcal/mol than in the singlet one at the periodic PW91 level (Table 3).

Two cases of a decrease in the energy differences  $\Delta U_{ST}$  between the singlet and triplet complexes containing  $O<sub>2</sub>$  species were already discussed in the literature [\[28,29\].](#page-9-0) The precise value of the small  $\Delta U_{ST}$  separation calculated using the MR-CISD method for the  $Li<sup>+</sup>O<sub>2</sub>$  complex is difficult to evaluate from the illustration in Ref. [\[28\]](#page-9-0). The molecular HO $_2^+$  cation is much better characterized by a rich series of accurate theoretical approaches, with a  $\Delta U_{ST}$  value around 4.45 ± 0.15 kcal/mol [\[29\],](#page-9-0) a much smaller value relative to the one for the  $O_2$  gas state (from 23.65 to 41.37 kcal/mol in upper line of Table 3).

To our best knowledge, only the MO<sub>X</sub>M clusters with  $X > 2$  are suspected as the centers that can accumulate  $^1O_2$  in various zeolites [\[28\]](#page-9-0). The stability of the singlet state (even if with a minor advantage of the triplet state) is in agreement with the fact that a singlet oxygen can thus be desorbed via a spin-allowed channel from the  ${}^{1}MO_{X}M$  to the  ${}^{1}MO_{X-N}M$  cluster while loosing  ${}^{1}O_{2}$ . Namely, this fact justifies our initial idea about the treatment of the singlet  $MO_XM$  clusters only [\[9,10\]](#page-9-0). The experimental facts prove that AEZ types also easily trap triplet oxygen [\[30\]](#page-9-0), which then can oxidize organics under thermal stimulation without additional source of oxygen. The last authors paid attention that the oxidation of propane takes place only after a preliminary treatment in air/oxygen atmosphere. But if the relatively easy  ${}^{1}O_{2}$  yield in AEZ obeys to spin conservation, then the  ${}^{3}O_{2}$  trapping reaction has to be also a spin-allowed process [\[30\]](#page-9-0). It suggests that the product of the  ${}^{1}MO_{X}M$  reaction with  ${}^{3}O_{2}$  has to possess a triplet  ${}^{3}MO_{X+2}M$  state in order to allow the  ${}^{3}O_{2}$  trapping. The closeness in energy and geometries between  ${}^{1}$ MO<sub>X+2</sub>M and  ${}^{3}$ MO<sub>W</sub> M<sub>1</sub> permits a fast transition from triplet  ${}^{3}$ MO<sub>W</sub> M<sub>1</sub> to singlet  ${}^{3}MO_{X+2}M$  permits a fast transition from triplet  ${}^{3}MO_{X+2}M$  to singlet  ${}^{1}MO_{X+2}M$  The similarities between the triplet and singlet energies  $1$ MO<sub>X+2</sub>M. The similarities between the triplet and singlet energies make less crucial the problem of the exact spin determination in the ground state. This question of spin distribution in zeolites seems to be directly related to the locally non-compensated charge distributions discussed recently [\[31\]](#page-9-0). Tentatively, the energies vary relatively slightly at the periodic level when the compensating cation or the  $GaO<sub>X</sub>Ga$  species located far from the substituting Al atom [\[31\]](#page-9-0). The problem of the closeness between the different multiplet states remains an interesting point for a future research requiring a powerful electron correlation method at the periodic level.

The low absolute  $\Delta U_{ST}$  values allow to check the thermodynamic possibility of the consequent oxidation steps between the singlet or triplet  $CaO<sub>X-1</sub>Ca$  and  $CaO<sub>X</sub>Ca$  species (X = 1–4) at the periodic level as it was done at the cluster level [\[9,10\].](#page-9-0) For example, for the reaction between the singlet states as we discussed before [\[9–11\]:](#page-9-0)

$$
{}^{1}MO_{X-1}M + 1/2{}^{3}O_{2} \rightarrow {}^{1}MO_{X}M
$$
 (1)

we got, for all X values and M = Ca, an exothermic  $\Delta U$  energy with the exception of  $X = 3$ , for which we got an endothermic effect of 1.38 kcal/mol (Table 3 and [Fig. 6](#page-6-0)). For the reaction  ${}^{1}$ CaOC $a(MOR) + {}^{3}O_{2} \rightarrow {}^{1}CaO_{3}Ca(MOR)$ , we observed an exothermic heat of  $(-14.04 + 1.38) = -12.66$  kcal/mol ([Fig. 6](#page-6-0)). Hence, all the CaO<sub>x</sub>Ca species for  $X = 1-4$  can be obtained and can react with  $CO<sub>2</sub>$ , as analyzed below.

3.2.2.1.2. MgO<sub>X</sub>Mg species in phillipsite (PHI). Even if the 8R window looks more distorted in PHI versus the one in the cluster 8R model (see Fig. 1 of [\[11\]](#page-9-0)), the angles and distances in the  $MgO<sub>2</sub>Mg$  moiety are nearly the same for both  $MgO<sub>2</sub>Mg(PHI)$  and  $MgO<sub>2</sub>Mg(8R)$ 

We added the Al atoms in the comparison because they are differently located around the  $MO_XM$  species in the MOR and PHI frameworks (Fig. 7). Hence, Al atoms could be responsible for the difference between the signs of the  $\Delta U_{ST}$  values between the MOR and PHI cases for  $X = 1$  or 2 at the periodic level. But they do not share the spin densities in both the cases.

<span id="page-5-0"></span>

Fig. 4. Optimized structures of the triplet CaOCa moieties in the (a and b) 8R and (c and d)  $6R + 4R$  clusters, respectively, as obtained at the (a and c) B3LYP/6-31G<sup>\*</sup> and (b and d) MP2/6-31G\* levels. The color code is the same as in [Fig. 1.](#page-1-0) (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

complexes. Details about their geometries are given in Ref. [\[11\].](#page-9-0) In this last paper, it was shown that  $MgO_xMg$  clusters possess a ground singlet state for  $X = 1-2$  and a ground triplet one for



Fig. 5. Projected spin densities of the singlet (open symbols) or triplet (closed symbols) states (PDOS) regarding the p-orbitals of the side O97 (a) atom in the  $O_3$ fragment of the singlet or triplet  $CaO<sub>3</sub>Ca$  state and (b) in the Ca–O97–Ca fragment in the singlet or triplet CaOCa +  $O_2$  states in MOR. The Fermi energy corresponds to zero. The location of the O97 atom in CaO<sub>3</sub>Ca is shown in [Fig. 6](#page-6-0).

 $X = 3-4$  at the level of the isolated 8R (Table 3 of Ref. [\[11\]](#page-9-0)) and  $6R + 4R$  clusters.<sup>8</sup> The  $\Delta U_{ST}$  values for  $X = 1-2$  could not be calculated at the B3LYP level because SCF convergence could not be achieved for both triplet states with  $X = 1-2$  for the isolated 8R and  $6R + 4R$  clusters. This non-convergence for the triplet states can also be considered as an evidence of their instability. At the MP2 level, the  $\Delta U_{ST}$  values are negative for  $X = 1-2$ , manifesting the favored singlet state. Let us add that the  $\Delta U_{ST}$  signs coincide at both MP2 and B3LYP levels as shown earlier for Ca clusters [\[10\]](#page-9-0).

Regarding the periodic results, we got a negative  $\Delta U = -9.01$  kcal/mol/cell<sup>9</sup> value for  $X = 2$ , thus suggesting the thermodynamic possibility of the  $MgO<sub>2</sub>Mg$  formation at the periodic level via the same reaction equation as Eq. [\(1\).](#page-4-0) The  $\Delta U_{ST}$  difference is indeed very small for MgOMg and MgO<sub>2</sub>Mg, suggesting clearly that the MgO<sub>x</sub>Mg species in singlet states can interact with  $CO<sub>2</sub>$  and form carbonates. All the carbonate species studied herein possess a singlet electronic ground state. Hence, their formation is not forbidden owing to the change of the total spin in the course of the interaction between  $MgO_XMg$  and CO<sub>2</sub>. The results of periodic calculations ([Table 3](#page-4-0)) show that the  $MgO_3Mg$  and  $MgO_4Mg$  moieties are characterized by positive  $\Delta U$  values, i.e., 21.10 and 21.68 kcal/mol/cell, respectively, so

<sup>&</sup>lt;sup>8</sup> The  $\Delta U_{ST}$  sign used in this present paper is inverted versus the one adopted in Refs. [\[9–11\].](#page-9-0)

 $9 -4.62$  kcal/mol ([Table 2](#page-3-0)) or  $-9.24$  kcal/mol/cell =  $(-413.710 + 403.543 +$  $9.766$ ) × 23.05 regarding two MgO<sub>X</sub>Mg species per cell.

<span id="page-6-0"></span>

**Fig. 6.** Optimized structures of the CaO<sub>X</sub>Ca clusters (X = 1–4) in MOR and heats of the CaO<sub>X–1</sub>Ca + ½<sup>3</sup>O<sub>2</sub>  $\rightarrow$  CaO<sub>X</sub>Ca reactions (kcal/mol) as calculated at the PDFT/PW91 level with VASP. The CaO<sub>x</sub>Ca moieties are shown by the ellipses. The color code is the same as in [Fig. 1.](#page-1-0) (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

that they are forbidden from thermodynamic point of view. Moreover, both  $MgO<sub>3</sub>Mg$  and  $MgO<sub>4</sub>Mg$  species are less stable than the  $MgO_XMg + O_2$  pairs for X = 1 or 2, respectively, and thus have to decompose.

The oxidation activity of Mg type zeolites can be related with the MgO<sub>2</sub>Mg formation. We also therefore considered the inverse reaction of the loss of singlet oxygen:

$$
{}^{1}MO_{2}M \to {}^{1}MOM + 1/2{}^{1}O_{2}
$$
 (2)

Singlet and triplet states are even more closer in energies for both MgOMg and MgO2Mg species in PHI than for the Ca analogs in MOR. We can thus admit that the reaction of oxygen trapping (3) is also spin allowed in MgPHI followed by a triplet to singlet transformation (4) owing to the similar geometry and energy:

$$
{}^{1}MOM + 1/2{}^{3}O_{2} \rightarrow {}^{3}MO_{2}M
$$
 (3)

$$
{}^{3}MO_{2}M \to {}^{1}MO_{2}M
$$
 (4)

The reasons for the smaller  $\Delta U_\mathrm{ST}$  energies in PHI relative to the ones in MOR remain non-clear. The comparison of the spin distributions in MOR and PHI did not show any Al participation which is symmetric and asymmetric in the MOR and PHI zeolites, respectively, near the  $MO_XM$  species. A partial answer about the possible role of the cation was obtained using analogous  $\Delta U_{ST}$  calculations in MgMOR. The  $\Delta U_{ST}$  energies are smaller than  $\Delta U_{ST}$  for CaMOR and are similar to the ones for MgPHI (Table 4). Hence, the selection of the cation is important for the absolute  $\Delta U_{ST}$  value. Let us note that this difference is, however, smaller than the precision of the calculations.

We can thus finally explain the oxidation activity of the Mg form zeolites by the  $MgO<sub>2</sub>Mg$  formation as already shown for the series of Ca clusters regarding the Ca forms [\[9,10\]](#page-9-0). The spe-

#### Table 4

Relative and absolute energies (eV) of the singlet ( $U<sub>S</sub>$ ) and triplet ( $U<sub>T</sub>$ ) states of the MOR unit cell including the  $MgO_XMg$  species, singlet-triplet energy differences  $(\Delta U_{ST} = U_S - U_T$ , kcal/mol), and  $\Delta U$  heats for reaction [\(1\)](#page-4-0) (kcal/mol) between singlet states using VASP (PW91) level.



cific property of the Mg forms relative to carbonate formation in the other AEZs is determined by the lower activation barrier of the chemisorption complex (15.3 kcal/mol) for CO oxidation obtained at the periodic level [\[11\].](#page-9-0) Such a complex was also optimized for the Zn forms with an activation energy of 23.6 kcal/mol at the cluster level [\[9\].](#page-9-0) For the other AEZs, we did not obtain a similar chemisorption complex, leading to the decrease in the activation energy.

3.2.2.2.  $CO<sub>2</sub>$  interaction with the  $MO<sub>X</sub>M(MOR)$  species. The geometries of the carbonate anions regarding  $CO<sub>2</sub>$  addition to the  $MO_XM(MOR)$  reagents ( $M = Mg$ , Ca) were calculated at the periodic level using VASP [\[13\]](#page-9-0) for the M forms of mordenite (MMOR) and the M forms of phillipsite (MPHI). The oxidation reaction sequence regarding the  $CaO<sub>x</sub>Ca(MOR)$  reagent structures from  $X = 1$  to 4 as optimized at the periodic level is presented in Fig. 6 and [Table 3.](#page-4-0) The  $MO_XM$  geometries obtained at the periodic level are pretty similar to the cluster ones obtained with B3LYP/6-31G\* [\[9–11\].](#page-9-0)

Regarding the  $CO<sub>2</sub>$  adsorption over the CaOCa(MOR) and CaCO<sub>3</sub>Ca(MOR) species, we obtained stable 3D structures with two frequencies with low absolute values, 1587.4 and  $1255.4$  cm<sup>-1</sup>, relative to 1648.8 and 1346.7 cm<sup>-1</sup> for the 8R cluster

<span id="page-7-0"></span>

**Fig. 7.** Optimized structures in the gas state: of the (a) transition state (the structures of the reagents and product in the gas state are simple and omitted for shortness), in the zeolite using CaCO<sub>3</sub>Ca(8R) moieties as source of CO<sub>2</sub>: of the (b) reagents, (c and f) intermediate states, and (d and e) products for the reaction between CO<sub>2</sub> and CH<sub>3</sub>OH<br>obtained at the B3LYP/6-31G\* level. The color c composition. Hydrogen bonds are shown by dotted lines. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

<span id="page-8-0"></span>model of MOR. Also, as mentioned above, any result coming from a theoretical approach leads to frequency values shifted relative to the experimental data; hence, we rescaled the calculated periodic PW91 values as the most strongly displaced ones relative to the experimental data. Fitting the symmetric vibration of  $1255.4$  cm<sup>-1</sup> to the "cluster" value of 1346.7 cm<sup>-1</sup>, instead of 1587.4  $cm^{-1}$ , we got a rescaled<sup>10</sup> asymmetric vibration of  $1666.8$  cm<sup>-1</sup> to be compared with the 8R cluster value of 1648.8 cm<sup>-1</sup> for MOR or the (6R + 4R) cluster value of 1664.0 cm<sup>-1</sup> for FAU [\(Table 2](#page-3-0)).

Regarding the interaction between the  $MO<sub>2</sub>M$  homologues and  $CO<sub>2</sub>$  at the periodic level, we did not succeed to obtain tri-dentate carbonate species as the ones optimized at the cluster level for MOR or FAU ([Fig. 2](#page-2-0)c and d). At the periodic level, we did not get any product of interaction between  $MO<sub>2</sub>M$  and  $CO<sub>2</sub>$  neither for MOR nor for PHI. We consider this as a confirmation that tri-dentate species ([Fig. 2c](#page-2-0) and d) do not appear in the AEZ forms. As well, it is indirectly confirmed by the absence of an upper frequency branch for the chemisorbed species, i.e., as calculated between 1860 and 1960  $\text{cm}^{-1}$  (X = 2 in [Table 2](#page-3-0)), in the experimental spectra of AEZ.

Similarly, we did not get any tri-dentate carbonate species via the periodic study for the interaction between  $CO<sub>2</sub>$  and the  $MO<sub>3</sub>M$  homologs. In this respect, the periodic model of  $CO<sub>2</sub>$  adsorption over  $CaO<sub>3</sub>Ca(MOR)$  species totally confirms the results of the cluster computations. The periodic model also led to the formation of an  $O_2$  fragment separated from CaCO<sub>3</sub>Ca(MOR) with bands at 1516.8 and 1225.5 cm<sup>-1</sup>. Rescaling the 1225.5 cm<sup>-1</sup> periodic value to the "cluster" one of  $1346.7 \text{ cm}^{-1}$ , we got, instead of 1516.8 cm<sup>-1</sup>, a rescaled value<sup>11</sup> of 1702.8 cm<sup>-1</sup> to be compared with the 8R cluster value of 1648.8 cm<sup>-1</sup> for MOR or the  $(6R + 4R)$ cluster one of 1664.0  $\text{cm}^{-1}$  for FAU ([Table 2\)](#page-3-0).

#### 4. Carbonate step in  $CO<sub>2</sub>$  activation

The relevance to consider the studied  $MCO<sub>3</sub>M$  systems toward the catalytic problems of  $CO<sub>2</sub>$  capture and reactivity can be discussed from many points of view. The most important one is the knowledge of a complete set of reactive sites that can be involved in the analyses of a selected process in cationic form zeolites. As we have mentioned above (see Section [3.2.1\)](#page-1-0), the presence of the carbonate species proves the existence of active  $MO_{x}M$  binuclear clusters in the AEZ forms. The MCO<sub>3</sub>M carbonates are fixed in the zeolite framework and do not move so that AEZ carbonate can appear when a  $MO_XM$  binuclear cluster exists already in the zeolite. The second additional advantage of the presented cluster moieties as potent catalytic system is the relation between the coordination number, three or four, of the carbonate and their IR spectra. The higher the energy difference between the low- and high-frequency branches, the closer the carbonate to the tri-dentate type. Similar coordinations could thus be proposed when doublets will be observed for a new zeolite system based on the doublet splitting. Third, it is clear that carbonate species can participate in many catalytic processes that include  $CO<sub>2</sub>$  binding. Such example can be shortly discussed keeping the main emphasis on the carbonate presence in the zeolites and their properties.

We considered the interaction between methanol and  $CO<sub>2</sub>$ , suggesting a similar activity for CaY as compared to CuY at elevated temperatures [\[32\]](#page-9-0). A gas-phase reaction can be proposed via a proton transfer step toward  $CO<sub>2</sub>$  with a heat of endothermic  $CH<sub>3</sub>HCO<sub>3</sub>$ formation evaluated as 11.5 kcal/mol at the same B3LYP/6-31G<sup>\*</sup> levels as was applied above in our work for the carbonate calculations. The activation energy in the gas phase is 42.3 kcal/mol, and the imaginary frequency is  $1699i$  cm<sup>-1</sup> in the transition state ([Fig. 7](#page-7-0)a). The favored orientation of  $CO<sub>2</sub>$  and CH<sub>3</sub>OH is determined by electrostatic interactions between the  $CO<sub>2</sub>$  quadrupole and  $CH<sub>3</sub>OH$  dipole so that the orientation is deeper by around of 1.3 kcal/mol than the  $O=C=O$ . H-OCH<sub>3</sub> geometry with hydrogen bonding.

The same reaction with methanol was repeated as in the gas phase but introducing the  $CaCO<sub>3</sub>Ca(8R)$  carbonate into the reactions instead of the gas-phase  $CO<sub>2</sub>$  molecule. The relevance of the Ca carbonate for the reaction can be confirmed by a slight exothermic effect of  $-3.7$  kcal/mol if one estimates the energy of the reagents involving the initial structure I ([Fig. 7](#page-7-0)b) and final product IV ([Fig. 7e](#page-7-0)). The energy of the reagent corresponds to the sum of the energy of the optimized structure I [\(Fig. 7](#page-7-0)b) containing two  $CH<sub>3</sub>OH$  molecules and the energy of an isolated  $CO<sub>2</sub>$  molecule at the same B3LYP/6-31G\* level. The energy of the product IV ([Fig. 7](#page-7-0)e) corresponds to the formation of dimethylcarbonate via a barrierless reaction with  $CO<sub>2</sub>$ , which restores the CaCO<sub>3</sub>Ca(8R) carbonate and hence completes the catalytic cycle. We will discuss only the first step of the reaction that leads to the  $CH_3CO_3^-$  anion formation as part of the complex III (5). [Fig. 7](#page-7-0) includes the energy values for all the models [\(Figs. 7](#page-7-0)b–d, f) with a similar chemical composition (with the exception of product IV that presents a two-step carbonylation as described above). The endothermic effect of the one-step reaction is smaller, 9.8 kcal/mol between structures I and III ([Fig. 7](#page-7-0)d), relative to the gas phase, 11.5 kcal/mol. However, we did not get the transition state (TS) that corresponds to the O-H breaking in methanol as in the gas-phase reaction. We obtained two intermediates II [\(Fig. 7](#page-7-0)c) and V [\(Fig. 7f](#page-7-0)) with energies lower than 40 kcal/mol, hence smaller than the activation energy in the gas phase (42.3 kcal/mol). It is very interesting to note that the carbon geometry in state II corresponds to a  $sp<sup>3</sup>$  hybridization while it is usually  $sp^2$  in the initial and final  $CO_3$  states. Both the II and V states can serve to look for the TS via the following mechanism as first step of dimethylcarbonate formation:

$$
\begin{aligned} \text{CaCO}_3\text{Ca}(8R) + 2\text{CH}_3\text{OH} &\rightarrow \text{Ca}(\text{CH}_3\text{O}^\circ\text{C}\text{O}_3\text{H})\text{Ca}(8R)^\circ \text{HOCH}_3(\text{II},\text{V}) \\ &\rightarrow \text{HO} - \text{Ca}(\text{CH}_3\text{CO}_3)\text{Ca}(8R)^\circ \text{HOCH}_3(\text{III}) \\ &\rightarrow \text{CH}_3\text{HCO}_3 + \text{CaOCa}(8R)^\circ \text{HOCH}_3 \end{aligned} \tag{5}
$$

The state II is especially promising as initial point for the proton transfer. However, the problem of localization of the TS at the cluster level met an obstacle created by the bending vibrations of the capping hydrogens of the 8R cluster. Owing to the fixed H atoms, the Si–H and Al–H frequencies are also imaginary. The reaction coordinate for the first step of dimethylcarbonate formation involves the motions of both the  $CH<sub>3</sub>O$  and OH groups that should result in a low imaginary frequency. We thus obtained a series of vibrations with imaginary frequencies below  $400i$  cm<sup>-1</sup> in which the contribution of the motion along the coordinate of methanol decomposition is relatively weak. We believe that calculations based on the use of periodic models could avoid this problem of the TS search with an activation energy lower than 40 kcal/mol. Such work is in progress. Nevertheless, the initial modeling step shows thus a perspective of carbonate inclusion into the reaction schemes for  $CO<sub>2</sub>$  binding and activation in AEZ type zeolites.

#### 5. Conclusions

Using cluster and periodic type DFT calculations, we demonstrated a clear correspondence between the experimental IR band positions and those calculated for tetra-dentate carbonate species between two cations within the  $MO_XM$  type species (M = Mg, Ca, Sr, Ba, with  $X = 1-4$ ) present in alkaline earth dehydrated zeolites. The frequencies of the theoretically obtained rigid  $MCO<sub>3</sub>M$ 

 $10$  (1346.7/1225.5)  $\times$  1516.8 = 1666.8 cm<sup>-1</sup>.

 $11$  (1346.7/1255.4)  $\times$  1587.4 = 1702.8 cm<sup>-1</sup>.

<span id="page-9-0"></span>structure remain nearly invariant versus the type of M cation or the type of framework in agreement with numerous experiments [1– 7]. Our models allow explaining the experimental intensity ratio [4] of the two bands presented in [Table 2.](#page-3-0) In all cases, the higher frequency, *i.e.*, 1600–1700  $\text{cm}^{-1}$ , corresponds to asymmetric carbonate vibrations, while the asymmetric/symmetric intensities result in comparable ratio versus the experimental ones. Two bands of asymmetric and symmetric vibrations for tri-dentate  $CO<sub>3</sub>$  with  $X = 2$  are outside the conventional range between 1800 and 1200  $\text{cm}^{-1}$  for carbonates [1-7]. Tri-dentate forms [\(Fig. 2](#page-2-0)c and d) do not appear in most of zeolite forms owing to their lower stability versus the tetra-dentate ones [9,10]. Our present work thus confirms that oxo-species serve as the source of oxygen for carbonate formation. Reactions including interaction between oxo-species and other small molecules will also be important at normal or high temperature conditions and need to be elucidated. Theoretical studies regarding such reactions are under progress. Our first results here presented relative to dimethylcarbonate formation with the CaCO<sub>3</sub>Ca carbonate as source of  $CO<sub>2</sub>$  demonstrate various intermediate states that can be considered as good initial points for the search of the transition states for reactions between carbonates and methanol under moderate temperatures.

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#### References

- [1] L. Bertsch, H.W. Habgood, J. Phys. Chem. 67 (1963) 1621.
- [2] J.W. Ward, H.W. Habgood, J. Phys. Chem. 70 (1966) 1178.
- [3] P.A. Jacobs, F.H. van Cauwelaert, E.F. Vansant, J.B. Uytterhoeven, J. Chem. Soc., Faraday Trans. I 69 (1973) 1056.
- [4] P.A. Jacobs, F.H. van Cauwelaert, E.F. Vansant, J. Chem. Soc., Faraday Trans. I 69 (1973) 2130.
- [5] G. Martra, S. Coluccia, P. Davit, E. Gianotti, L. Marchese, H. Tsuji, H. Hattori, Res. Chem. Intermed. 25 (1999) 77.
- [6] F.X. Llabrers i Xamena, A. Zecchina, Phys. Chem. Chem. Phys. 4 (2002) 1978.
- [7] J.V. Evans, T.L. Whateley, Trans. Faraday Soc. 63 (1967) 2769.
- [8] L.H. Little, Infrared Spectra of Adsorbed Species, Academic Press, New York, 1966.
- [9] G.M. Zhidomirov, A.V. Larin, D.N. Trubnikov, D.P. Vercauteren, J. Phys. Chem. C 113 (2009) 8258. [10] A.V. Larin, G.M. Zhidomirov, D.N. Trubnikov, D.P. Vercauteren, J. Comput.
- Chem. 31 (2010) 421.
- [11] A.A. Rybakov, A.V. Larin, G.M. Zhidomirov, D.N. Trubnikov, D.P. Vercauteren, Comput. Theor. Chem. 964 (2011) 108.
- [12] M.J. Frisch, G.W. Trucks, H.B. Schlegel, G.E. Scuseria, M.A. Robb, J.R. Cheeseman, J.A. Montgomery Jr., T. Vreven, K.N. Kudin, J.C. Burant, J.M. Millam, S.S. Iyengar, J. Tomasi, V. Barone, B. Mennucci, M. Cossi, G. Scalmani, N. Rega, G.A. Petersson, H. Nakatsuji, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, M. Klene, X. Li, J.E. Knox, H.P. Hratchian, J.B. Cross, V. Bakken, C. Adamo, J. Jaramillo, R. Gomperts, R.E. Stratmann, O. Yazyev, A.J. Austin, R. Cammi, C. Pomelli, J.W. Ochterski, P.Y. Ayala, K. Morokuma, G.A. Voth, P. Salvador, J.J. Dannenberg, V.G. Zakrzewski, S. Dapprich, A.D. Daniels, M.C. Strain, O. Farkas, D.K. Malick, A.D. Rabuck, K. Raghavachari, J.B. Foresman, J.V. Ortiz, Q. Cui, A.G. Baboul, S. Clifford, J. Cioslowski, B.B. Stefanov, G. Liu, A. Liashenko, P. Piskorz, I. Komaromi, R.L. Martin, D.J. Fox, T. Keith, M.A. Al-Laham, C.Y. Peng, A. Nanayakkara, M. Challacombe, P.M.W. Gill, B. Johnson, W. Chen, M.W. Wong, C. Gonzalez, J.A. Pople, Gaussian 03, Revision C.02, Gaussian, Inc., Wallingford, CT, 2004.
- [13] (a) G. Kresse, J. Hafner, Phys. Rev. B 47 (1993) 558;
- (b) G. Kresse, J. Furthmüller, Phys. Rev. B 54 (1996) 11169.
- [14] G. Kresse, J. Joubert, Phys. Rev. B 59 (1999) 1758. [15] (a) J.P. Perdew, J.A. Chevary, S.H. Vosko, K.A. Jackson, M.R. Pederson, D.J. Singh, C. Fiolhais, Phys. Rev. B 46 (1992) 6671;
- (b) J.P. Perdew, K. Burke, M. Ernzerhof, Phys. Rev. Lett. 77 (1996) 3865.
- [16] P. Ugliengo, D. Viterbo, G. Chiari, Z. Kristall. 207 (1993) 9.
- [17] E. Garrone, B. Bonelli, C. Lamberti, B. Civalleri, M. Rocchia, P. Roy, C. Otero Areán, J. Chem. Phys. 117 (2002) 10274.
- [18] N.D. Parkyns, J. Chem. Soc. A (1969) 410.
- [19] A. Brunet-Bruneau, D. Souche, S. Fisson, V. Nguyen Van, G. Vuye, F. Abeles, J. Rivory, J. Vac. Sci. Technol. A 16 (1998) 2281.
- [20] Q.L. Liu, A. Mace, Z. Bacsik, J.L. Sun, A. Laaksonen, N. Hedin, Chem. Commun. 46 (2010) 4502.
- [21] H.A. Aleksandrov, G.N. Vayssilov, N. Rösch, J. Mol. Catal. A 256 (2006) 149.
- [22] R.F.W. Bader, Atoms in Molecules: A Quantum Theory; The International Series
- of Monographs in Chemistry, Clarendon Press, Oxford, UK, 1995. [23] A.V. Larin, A. Mace, A.A. Rybakov, Z. Bacsik, N. Hedin, A. Laaksonen, in preparation.
- [24] N. Rane, A.R. Overweg, V.B. Kazansky, R.A. van Santen, E.J.M. Hensen, J. Catal. 239 (2006) 478.
- [25] D.F. Plant, G. Maurin, H. Jobic, P.L. Llewellyn, J. Phys. Chem. B 110 (2006) 14372.
- [26] T. Montanari, G. Busca, Vib. Spectrosc. 46 (2008) 45.
- [27] A.V. Larin, A.A. Rybakov, G.M. Zhidomirov, A. Mace, A. Laaksonen, D.P. Vercauteren, Theoretical modeling of carbonate formation in dehydrated alkaline earth zeolites, ACS 239th National Meeting, Division of Fuel Chemistry, San Francisco, CA, USA, 21-25.3.2010, ID 26896.
- [28] O.V. Udalova, E.V. Khaula, M.Y. Bykhovskii, Y.N. Rufov, A.N. Romanov, Russ. J. Phys. Chem. 77 (2003) 912.
- [29] X. Huang, T.J. Lee, J. Chem. Phys. 129 (2008) 044312.
- [30] J. Xu, B.L. Mojet, J.G. van Ommen, L. Lefferts, J. Phys. Chem. B 109 (2005) 18361.
- [31] E.A. Pidko, E.J.M. Hensen, G.M. Zhidomirov, R.A. van Santen, J. Catal. 255 (2008) 139.
- [32] G. Rebmann, V. Keller, M.J. Ledoux, N. Keller, Green Chem. 10 (2008) 207.